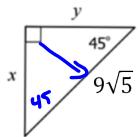


Warm Up:

$$1. \quad x = \underline{4\sqrt{10}}$$

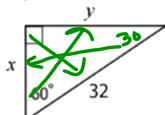
$$y = \underline{4\sqrt{10}}$$



30	60	90
X	$x\sqrt{3}$	$2x$

$$2. \quad x = \underline{16}$$

$$y = \underline{16\sqrt{3}}$$



16	$16\sqrt{3}$	32
----	--------------	----

$$3. \quad \text{Simplify.} \quad 6a^{\frac{2}{5}} \cdot 2a^{\frac{3}{4}} = \underline{12a^{\frac{23}{20}}}$$

Right Triangle Trigonometry

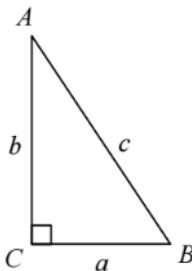
(Finding Missing Sides)

If you have a triangle that its angles are different than 30° , 45° , 90° how you can solve for the missing side?

You can use trigonometric ratios
 \sin , \cos , and \tan

May 11-9:56 AM

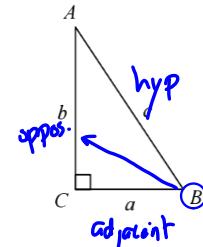
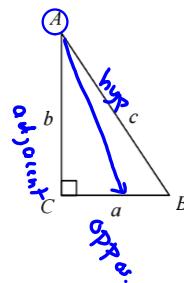
May 11-9:42 AM



Notation for the angles and sides:

Angles are in UPPERCASE;
 side opposite an angle has
 the same letter, but in
lowercase

What do we mean by opposite and adjacent sides?



Dec 5-3:16 PM

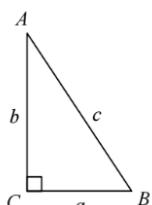
Dec 5-4:02 PM

New! Trigonometric Ratios

name	abbreviation
sine	sin
cosine	cos
tangent	tan

SINE

The ratio of the leg **opposite** the angle to the **hypotenuse**.



$$\sin A = \frac{?}{c}$$

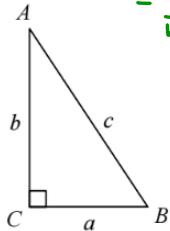
$$\sin B = \frac{?}{c}$$

Dec 5-3:17 PM

May 11-9:44 AM

COSINE

The ratio of the leg **adjacent** to the angle to the **hypotenuse**.



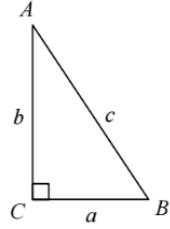
$$= \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\cos A = \frac{b}{c}$$

$$\cos B = \frac{a}{c}$$

TANGENT

The ratio of the leg **opposite** the angle to the leg **adjacent** to the angle.



$$\tan A = \frac{b}{a}$$

$$\tan B = \frac{a}{b}$$

May 11-9:44 AM

May 11-9:44 AM

Remember !!

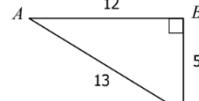
SOH - CAH - TOA

$$\sin = \frac{\text{opp}}{\text{hyp}}$$

$$\cos = \frac{\text{adj}}{\text{hyp}}$$

$$\tan = \frac{\text{opp}}{\text{adj}}$$

Example: Write the ratios in simplest form.



$$\bullet \sin A = \frac{5}{13}$$

$$\bullet \cos A = \frac{12}{13}$$

$$\bullet \tan A = \frac{5}{12}$$

$$\bullet \sin C = \frac{12}{13}$$

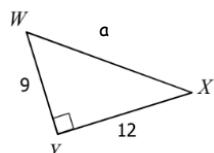
$$\bullet \cos C = \frac{5}{13}$$

$$\bullet \tan C = \frac{12}{5}$$

May 11-9:46 AM

May 11-9:47 AM

Example: Write the ratios in simplest form.



$$\bullet \sin W = \frac{9}{a}$$

$$\bullet \sin X = \frac{9}{a}$$

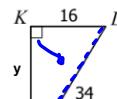
$$\bullet \cos W = \frac{a}{9}$$

$$\bullet \cos X = \frac{12}{a}$$

$$\bullet \tan W = \frac{9}{\sqrt{a^2 - 81}}$$

$$\bullet \tan X = \frac{9}{12}$$

Example: You try! Write the ratios in simplest form.



$$\bullet \sin L = \frac{y}{34}$$

$$\bullet \cos L = \frac{16}{\sqrt{y^2 + 16^2}}$$

$$\bullet \tan L = \frac{y}{16}$$

$$\bullet \sin M = \frac{16 - y}{\sqrt{y^2 + 16^2}}$$

$$\bullet \cos M = \frac{y}{\sqrt{y^2 + 16^2}}$$

$$\bullet \tan M = \frac{16 - y}{y}$$

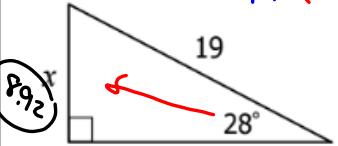
May 11-9:48 AM

May 11-9:49 AM

Example: Solve for the missing side.

Make sure your calculator is in
DEGREE MODE!

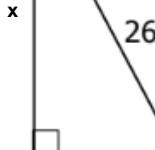
$$19 \cdot (\sin 28^\circ) = \frac{x}{19}$$



$$8.92 \approx x$$

Example: Solve for the missing side.

$$26 \cdot (\cos 21^\circ) = \frac{x}{26}$$

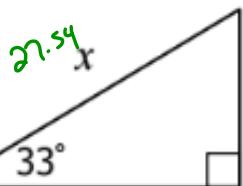


$$24.27 \approx x$$

May 11-9:51 AM

May 11-9:51 AM

Example: Solve for the missing side.



$$\begin{aligned} x(\sin 33^\circ) &= \frac{15}{x} \\ x \cdot (\sin 33^\circ) &= 15 \\ \frac{x \cdot (\sin 33^\circ)}{\sin 33^\circ} &= \frac{15}{\sin 33^\circ} \\ x &= 27.54 \end{aligned}$$

Example: Solve for the missing side.

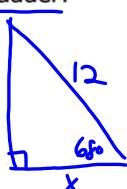
$$\begin{aligned} 11 &\quad x \cdot (\tan 64^\circ) = \frac{11}{x} \\ 64^\circ &\quad x \cdot (\tan 64^\circ) = 11 \\ \frac{x \cdot (\tan 64^\circ)}{\tan 64} &= \frac{11}{\tan 64} \\ x &\approx 5.36 \end{aligned}$$

May 11-9:51 AM

May 11-9:51 AM

Example:

Jake leaned a 12-foot ladder against his house. If the angle formed by the ladder and the ground is 68° , how far from the base of the house did he place the ladder?

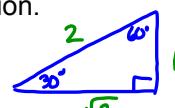


$$12 \cdot (\cos 68^\circ) = \frac{x}{12}$$

$$4.49 \approx x$$

Use special right triangles to write each trig ratio as a simplified fraction.

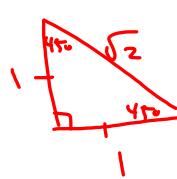
$$1) \sin 30^\circ = \frac{1}{2}$$



$$2) \cos 30^\circ = \frac{\sqrt{3}}{2}$$

30	60	90
x	$x\sqrt{3}$	$2x$
1	$\sqrt{3}$	2

$$3) \tan 45^\circ = 1$$



45	45	90
x	x	$x\sqrt{2}$
1	1	$\sqrt{2}$

May 11-9:54 AM

Dec 6-7:31 AM