

Warm-up

Solve by completing the square

1) $x^2 + 18x = 7$

2) Simplify $\left(\frac{a^3}{b}\right)^{-1}$

Sep 27-7:10 AM

Methods to Solve Quadratic Equations

Always works!

1) Completing the Square

2) Quadratic Formula

3) Factoring

4) Finding zeros

5 Taking square roots of each side

Today ✓

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Method 1:

By Completing the Square

(Always works, but can be messy if we "half-it, square-it" and have fractions to work with.)

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Method 2:

By Quadratic formula

(Always works)

$$X = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

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Method 3: Solve by Factoring

Works as long as the quadratic expression is **factorable**

$$a^2 - b^2 = (a - b)(a + b)$$

$$a^2 - 2ab + b^2 = (a - b)^2$$

$$a^2 + 2ab + b^2 = (a + b)^2$$

X X, X X → * * * (3 terms)
grouping
Sum & product $ax^2 + bx + c$
 $a = \dots, b = \dots, c = \dots$
 $a \times c \mid b \text{ (order)}$
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Method 4:

Solve quadratics by taking square roots

Form: $ax^2 + c = 0$ (usually **missing the bx** term)

1) $x^2 - 49 = 0$

$$x^2 = 49$$

$$\sqrt{x^2} = \sqrt{49}$$

$$x = \pm 7 \rightarrow x = 7, x = -7$$

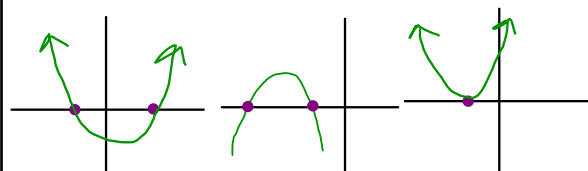
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2) $2x^2 + 100 = 0$ $\sqrt{x^2} = \sqrt{50}$
 $2x^2 = -100$ $x = \sqrt{-1(2)(25)}$
 $x^2 = -50$

3) $(x-5)^2 = 81$ $x = \pm 5 \pm \sqrt{81}$
 $\sqrt{(x-5)^2} = \sqrt{81}$
 $x-5 = \pm 9$
 $x-5 = 9$ $x-5 = -9$
 $x = 14$ $x = -4$

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Method 5: Solve quadratics by graphing and find the 'zeros'



*Works when there are x-intercepts. May only get a decimal estimation of the actual solutions

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Use your calculator to find the roots.

1) $x^2 - 5x + 2 = 0$

Slide to reveal

2) $-3x^2 - 5x + 12 = -8$

Slide to reveal

3) $x^2 = -2x + 7$

Slide to reveal

4) $x^2 + 3 = 0$

Slide to reveal

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Practice

...then short quiz

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Operations on Imaginary Numbers

$a + bi$
 Real Part Imaginary Part

$3 + 2i$

$$\begin{aligned} i &= \sqrt{-1} \\ i^2 &= (\sqrt{-1})^2 = -1 \end{aligned}$$

Add

$$\begin{aligned} &(3 + 6i) + (5 - 3i) \\ &= 8 + 3i \end{aligned}$$

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Multiplication

$$(3 + 2i)(5 - 4i)$$

$$= 15 - 12i + 10i - 8i^2$$

$$= 15 - 12i + 10i - 8(-1)$$

$$= 15 - 2i + 8$$

$$= 23 - 2i$$

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Solve by Completing the Square.

$$1- K^2 - 8K = -14 \quad \square = \left(\frac{b}{2}\right)^2$$

$$K^2 - 8K + 16 = -14 + 16 \quad b = -8$$

$$(K-4)^2 = 2$$

$$\square = \left(\frac{-8}{2}\right)^2$$
$$= (-4)^2$$
$$= 16$$

$$\sqrt{(K-4)^2} = \sqrt{2}$$

$$K-4 = \pm 1.4$$

$$K = 4 + 1.4 = 5.4$$

$$K = 4 - 1.4 = 2.6$$

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