

Warm-up:

Use the calculator to find the zeros
(Round to hundredths place)

$$1) 3x^2 + 5x - 10 = 0$$

$$2) x^2 - 6x = -9$$

$$3) x^2 + 3 = 0$$

Oct 11-4:23 PM

Warm-up: Simplify each.

$$1) \sqrt{20} = 2\sqrt{5}$$

$$4) \sqrt{49} = 7$$

$$2) -5\sqrt{72}$$

$$5) -\sqrt{49} = -7$$

$$3) \sqrt{588} = \cancel{-5}(2)\sqrt{18}$$

$$= -10\sqrt{18}$$

$$\times$$

$$6) \sqrt{549}$$

$$= \sqrt{1}\sqrt{49}$$

$$(*7)$$

$$= 7$$

Aug 8-9:20 AM

Solving Quadratic Equations

$$ax^2 + bx + c = 0$$

Methods

- 1) Completing the Square ~~✓~~
- 2) Quadratic Formula ✓
- 3) Factoring ✓
- 4) Taking Square roots
- 5) Finding zeros in calculator

Sep 24-8:11 PM

All quadratic equations can be solved, but not all quadratic equations have **real** solutions. What does that mean???

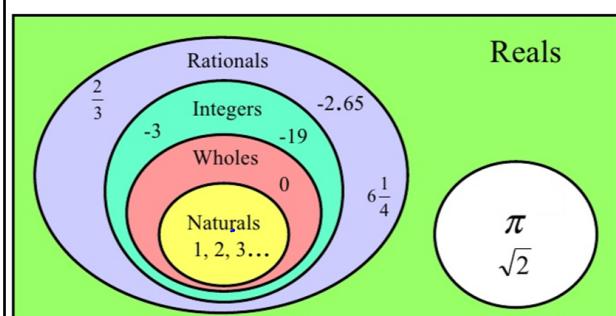
In order to solve all quadratic equations, we will need to step into the **Complex Number System**

....First, let's see if we remember what makes up the **Real Number System**

Sep 18-9:05 PM

Choose from: Wholes, Naturals, Rational, Irrational, Reals, Integers

Real Number System



Jan 19-4:12 PM

Remember $\sqrt{-1}$ in real number system?

It was undefined

Now...into the complex number system.

$\sqrt{-1}$: No longer undefined...it gets a name!

$$\begin{aligned} i &= \sqrt{-1} \quad i^2 = -1 \\ (i^2)^2 &= \sqrt{-1} \cdot \sqrt{-1} \end{aligned}$$

Feb 25-3:58 PM

and it's name is...

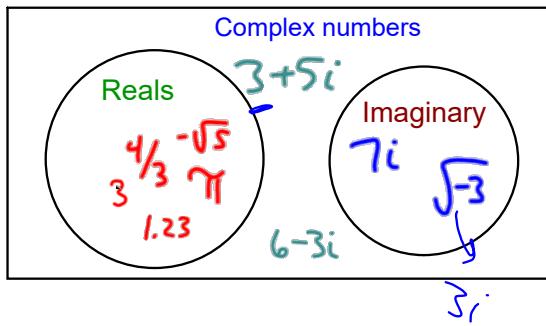
$$i = \sqrt{-1}$$

Complex number: Form $a + bi$

real part
imaginary part

Feb 25-4:00 PM

Complex Number System



Feb 25-4:00 PM

A) Simplify

$$\begin{aligned} \sqrt{a \cdot b} &= \sqrt{a} \sqrt{b} \\ 1) \sqrt{-25} &= \sqrt{-1(25)} = \sqrt{-1} \sqrt{25} = 5i \\ 2) 10\sqrt{-72} &= 10\sqrt{-1(72)} = 10\sqrt{-1} \sqrt{4} \sqrt{18} \\ 3) \frac{2 + \sqrt{-75}}{2 + 5i\sqrt{3}} &= 20i\sqrt{18} \\ 4) -5\sqrt{-18} &= -5\sqrt{-1(9)(2)} \\ &= -5(3)i\sqrt{2} = -15i\sqrt{2} \end{aligned}$$

Feb 25-4:08 PM

Solving Quadratics by Completing the Square ✓

If and only if $a=1$

$$9x^2 + bx + c = 0$$

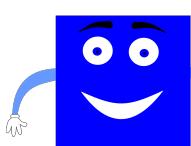
\uparrow
 $= 1$

Sep 18-9:08 PM

First, we need to know what a **perfect square trinomial** is and how to create one

Sep 24-8:21 PM

What is a "perfect square trinomial" ??



$$\begin{aligned} a^2 - 2ab + b^2 &= (a-b)^2 \\ x^2 - 16x + 64 &= (x-8)^2 \end{aligned}$$

$$\begin{aligned} \sqrt{x^2} &= x = a \\ \sqrt{64} &= 8 = b \\ 2ab &= 16x \\ &= (x-8)^2 \end{aligned}$$

Sep 24-8:25 PM

Now... Make a perfect square trinomial

$$\begin{aligned} ax^2 + bx + c & \\ 1) x^2 + 10x + 25 & \quad a=x, b=10, c=25 \quad \square = \left(\frac{b}{2}\right)^2 \\ a^2 + 2ab + b^2 & \\ (x+5)^2 & \quad b=5 \quad \left(\frac{10}{2}\right)^2 \\ 2) x^2 - 16x + 64 & \quad a=x, b=-16, c=64 \quad \square = \left(\frac{-16}{2}\right)^2 \\ a^2 - 2ab + b^2 & \\ (x-8)^2 & \quad b=8 \quad \left(\frac{-16}{2}\right)^2 \\ 3) x^2 - 5x + 25/4 & \quad a=x, b=-5, c=25/4 \quad \square = \left(\frac{5}{2}\right)^2 \\ (x-\frac{5}{2})^2 & \quad b=8 \quad \left(\frac{5}{2}\right)^2 \end{aligned}$$

Oct 1-8:35 AM

Solve by completing the square

$$\begin{aligned} 1) x^2 - 6x - 40 &= 0 \quad \square = \left(\frac{b}{2}\right)^2 \\ a=1 & \\ x^2 - 6x &= 40 \quad \square = \left(\frac{-6}{2}\right)^2 \\ x^2 - 6x + 9 &= 40 + 9 \quad \square = \left(\frac{-6}{2}\right)^2 \\ x^2 - 6x + 9 &= 49 \quad \square = 9 \\ \sqrt{x^2} &= x = a \rightarrow \sqrt{9} = 3 = b \\ a^2 - 2ab + b^2 &= (a-b)^2 \\ (x-3)^2 &= 49 \\ \sqrt{(x-3)^2} &= \sqrt{49} \\ x-3 &= \pm 7 \\ x-3 = 7 & \quad | \quad x-3 = -7 \\ x = 10 & \quad | \quad x = -4 \end{aligned}$$

Oct 2-9:05 AM

$$\begin{aligned} 2) x^2 + 12x + 4 &= 0 \quad \square = \left(\frac{b}{2}\right)^2 \\ x^2 + 12x &= -4 \quad \square = \left(\frac{12}{2}\right)^2 \\ x^2 + 12x + 36 &= -4 + 36 \quad \square = \left(\frac{12}{2}\right)^2 = 36 \\ a^2 + 2ab + b^2 &= (a+b)^2 \\ a=x, b=6 & \\ (x+6)^2 &= 36 \\ \sqrt{(x+6)^2} &= \sqrt{36} \quad x+6 = 6 \\ x+6 &= \pm 6 \quad \text{or } x+6 = -6 \\ x = 0 & \quad | \quad x = -12 \\ x = 6 & \quad | \quad x = -6 \end{aligned}$$

Oct 2-9:10 AM

$$3) x^2 + 12x + 7 = 6$$

Now try to do it by yourself !

Oct 2-9:13 AM

$$4) 2x^2 - 20x + 10 = 0$$

More practice

Sep 18-8:57 PM

$$5) \ x^2 + 2x + 3 = -5$$

Oct 2-12:50 PM

$$6) \ x^2 + 8x + 31 = 6$$

Mar 5-4:57 PM

$$7) \ 2x^2 - 12x + 6 = 0$$

Sep 24-8:31 PM